

ELASTICITY THEORY SOLUTION OF THE PROBLEM ON PLANE BENDING OF A NARROW LAYERED CANTILEVER BEAM BY LOADS AT ITS FREE END

A. V. Goryk* and S. B. Koval'chuk

Keywords: *beam, composite, layer, bending, stresses, strains, displacements*

An exact elasticity theory solution for the problem on plane bending of a narrow layered composite cantilever beam by tangential and normal loads distributed on its free end is presented. Components of the stress-strain state are found for the whole layers package by directly integrating differential equations of the plane elasticity theory problem by using an analytic representation of piecewise constant functions of the mechanical characteristics of layer materials. The continuous solution obtained is realized for a four-layer beam with account of kinematic boundary conditions simulating the rigid fixation of its one end. The solution obtained allows one to predict the strength and stiffness of composite cantilever beams and to construct applied analytical solutions for various problems on the elastic bending of layered beams.

Introduction

[REDACTED]

Poltava State Agrarian Academy, Poltava, Ukraine

*Corresponding author; e-mail: oleksii.goruk@pdaa.edu.ua

Translated from *Mekhanika Kompozitnykh Materialov*, Vol. 54, No. 2, pp. 269-284, March-April, 2018. Original article submitted August 4, 2017.

REFERENCES

1. H. Altenbach, "Theories for laminated and sandwich plates. A review," *Mech. Compos. Mater.*, **34**, No. 3, 243-252 (1998).
2. S. A. Ambartsumyan, *Theory of Anisotropic Plates* [in Russian], Nauka, Moscow (1987).
3. V. V. Bolotin and Yu. N. Novitchkov, *Mechanics of Multilayered Structures* [in Russian], Mashinostroyenie, Moscow (1980).
4. V. V. Vasil'yev, *Mechanics of Structures from Composite Materials* [in Russian], Mashinostroyenie, Moscow (1988).
5. V. G. Piskunov, A. V. Gorik, A. L. Lyakhov, and V. M. Cherednikov, "High-order model of the stress-strain state of composite bars and its implementation by computer algebra," *Compos. Struct.*, **48**, Iss. 1-3, 169-176 (2000), doi: 10.1016/S0263-8223(99)00091-4.
6. E. I. Grigolyuk and I. T. Selezov, *Nonclassical Vibration Theory of Bars, Plates, and Shells. Results of Science and Technics* [in Russian], **5**, Nauka, Moscow (1972).
7. A. N. Guz', Ya. M. Grigorenko, G. A. Vanin, and I. Yu. Babich, *Mechanics of Structural Elements*, **2**, *Mechanics of Composite Materials and Structural Elements* [in Russian], Naukova Dumka, Kiev (1983).
8. A. K. Malmeister, V. P. Tamuzh, and G. A. Teters, *Strength of Polymer and Composite Materials* [in Russian], Zinatne, Riga (1980).
9. V. G. Piskunov, "An iterative analytical theory in the mechanics layered composite systems," *Mech. Compos. Mater.*, **39**, No. 1, 2-24. (2003).
10. V. G. Piskunov and V. E. Verizhenko, *Linear and Nonlinear Problems of Calculation of Layered Structures* [in Russian], Budivel'nik, Kiev (1986).
11. A. O. Rasskazov, I. I. Sokolovskaya, and N. A. Shul'ga, *Theory and Calculation of Laminated Orthotropic Plates and Shells* [in Russian], Visha Shkola, Kiev (1987).
12. S. G. Lekhnitskij, *Elasticity Theory of an Anisotropic Bodies* [in Russian], Nauka, Moscow (1977).
13. A. V. Marchuk, "Three-dimensional analytical solution," *Prikl. Mekh.*, **33**, No. 9, 10-14 (1997).

14. N. I. Muskhelishvili, Some Fundamentals Problems of the Mathematical Theory of Elasticity [in Russian], Nauka, Moscow (1966).
15. N. J. Pagano, "Exact solutions for composite laminates in cylindrical bending," J. Compos. Mater., **3**, No. 3, 398–411 (1969).
16. Pagano N. J. "Exact solutions for rectangular bidirectional composites," J. Compos. Mater., **4**, No. 1, 20-34 (1970).